



## A smart scheduling algorithm for a decentralized energy management system

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Chair of Communication Networks

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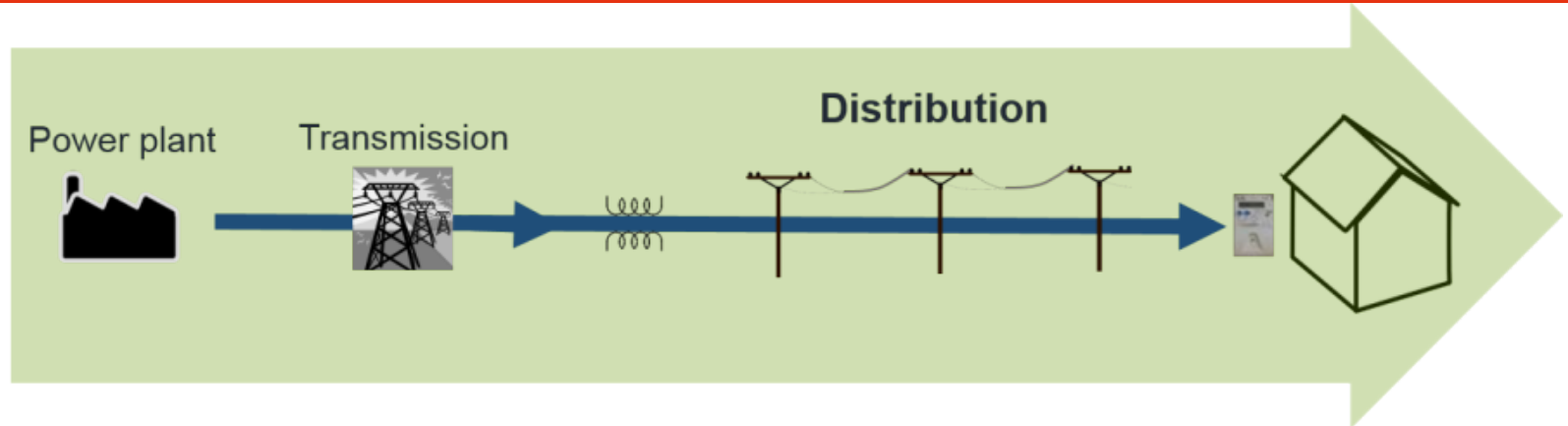
**Prof. Dr.-Ing. Thomas Bauschert**

TU Chemnitz ,  
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**Dr.-Ing Dipl.-Math. Andreas**

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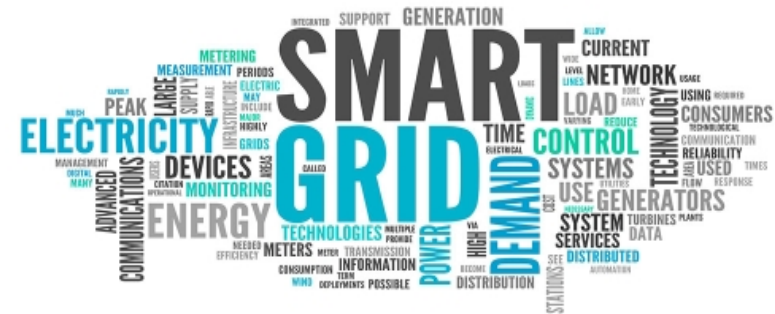
1. Motivation
2. Outline of algorithm
3. Prediction phase or phase 1
4. Optimization phase or phase 2
5. Results of the proposed algorithm
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7. Inference and Conclusion



*Fig 1. Traditional Electrical Grid [1]*

## Current problems

- Infrastructure problems
  - Black outs
  - Brown outs
  - High cost
- Inflexibility
- Lack of information transparency



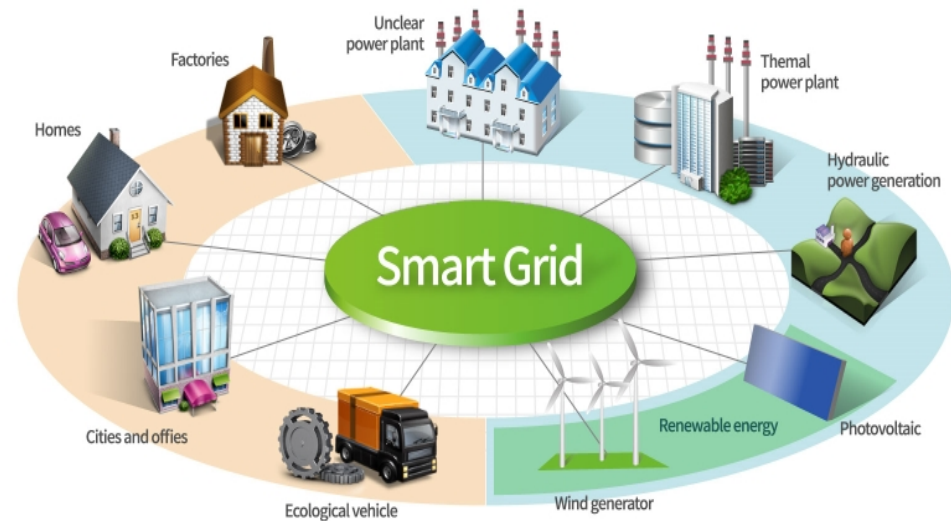
**Upcoming challenges** :Scarcity of resources, Distributed power supply  
Automated control through out the grid

## Supporting technologies

- Real time pricing
- Advance meter reading : AMI or Automated meter reading : AMR
- Enable Home area network : HAN

## Characteristics of HAN

- Motivates the customers
  - Modified COEC
  - Real time demand-pricing information
  - Low installation cost
  - Reduced system peak
  - Efficient and smart appliances
- Resist Attack
- Accommodate all the generation and storage options
- Optimize the assets and operates efficiently
- Smart in-home system



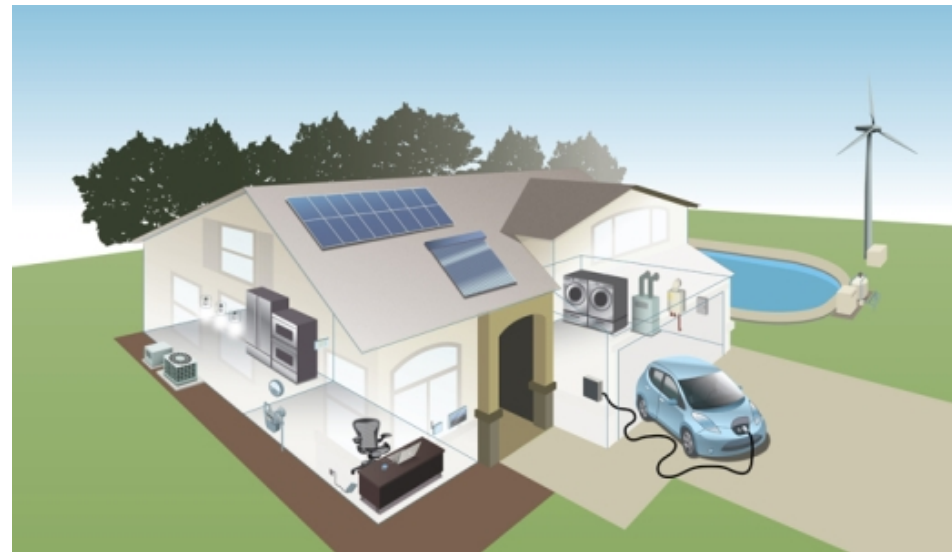
**Fig 2. Smart Grid [2]**

## Supporting technologies

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**Fig 2. HAN [3]**

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## 3 Phases of algorithm

### Prediction Phase / Phase 1

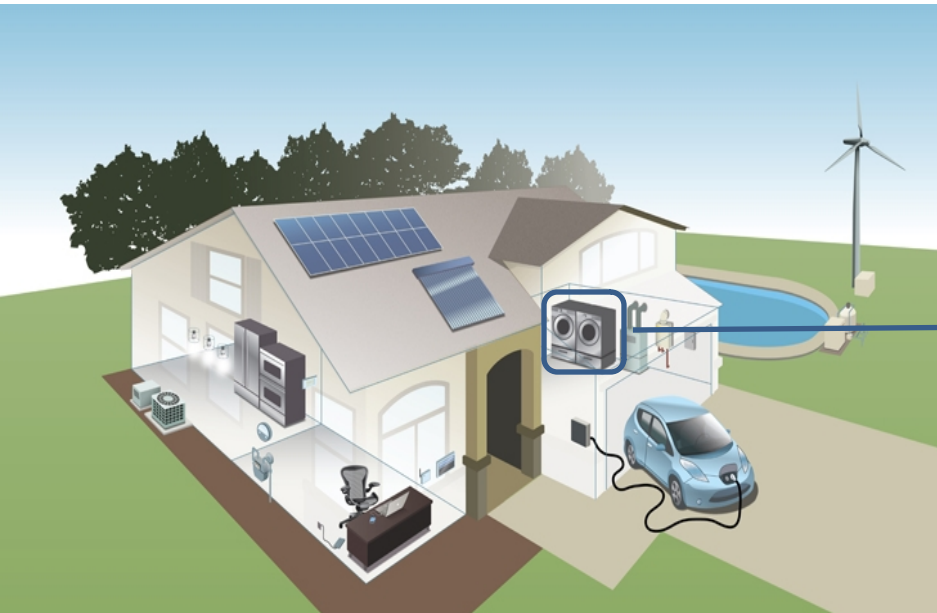
Predict next 24h device switching pattern and electricity price information .

### Optimization Phase / Phase 2

The objective of this phase is to optimize the forecasted switching patterns (ON-OFF patterns)

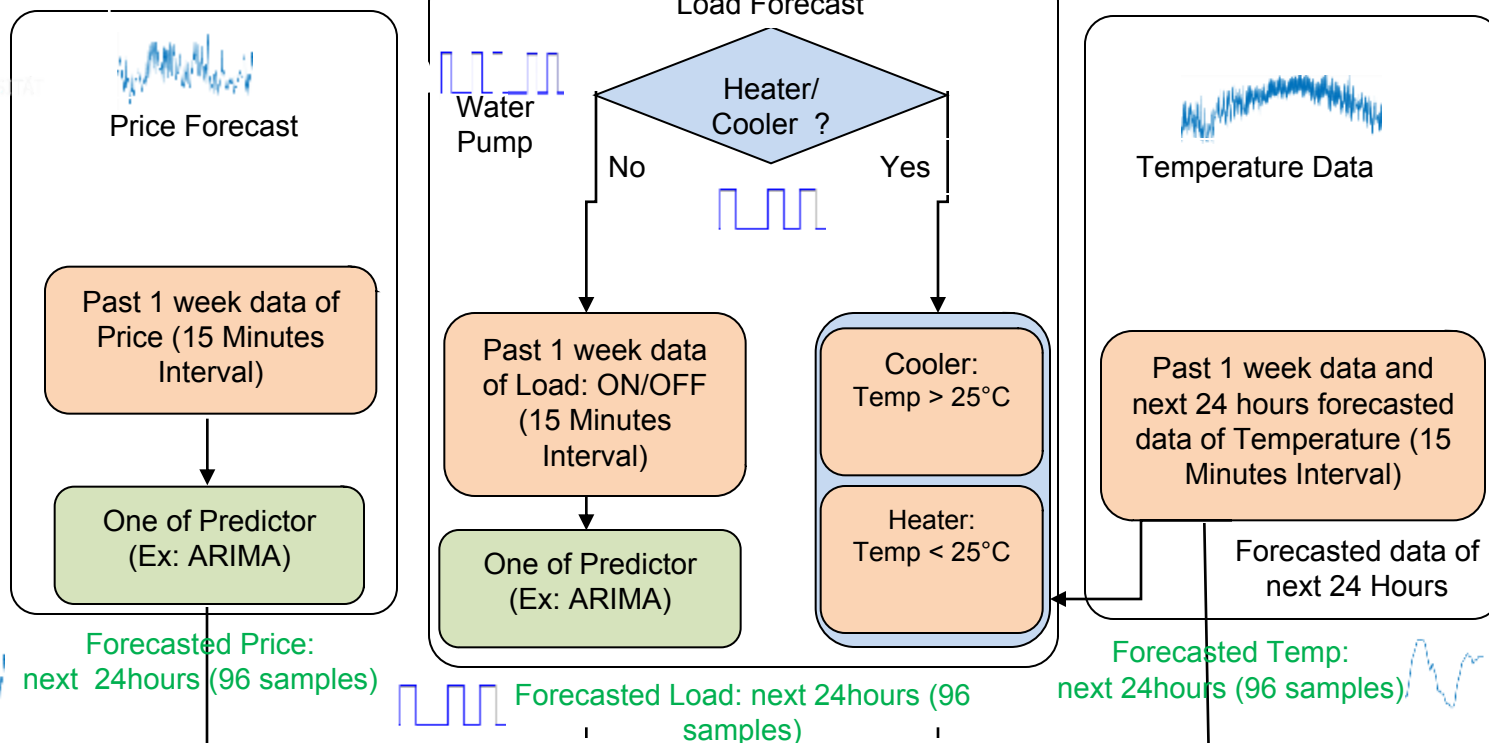
### Phase 3

Once the device switching schedule is optimized in phase 2, the controller hardware takes over, to control the device state of operation

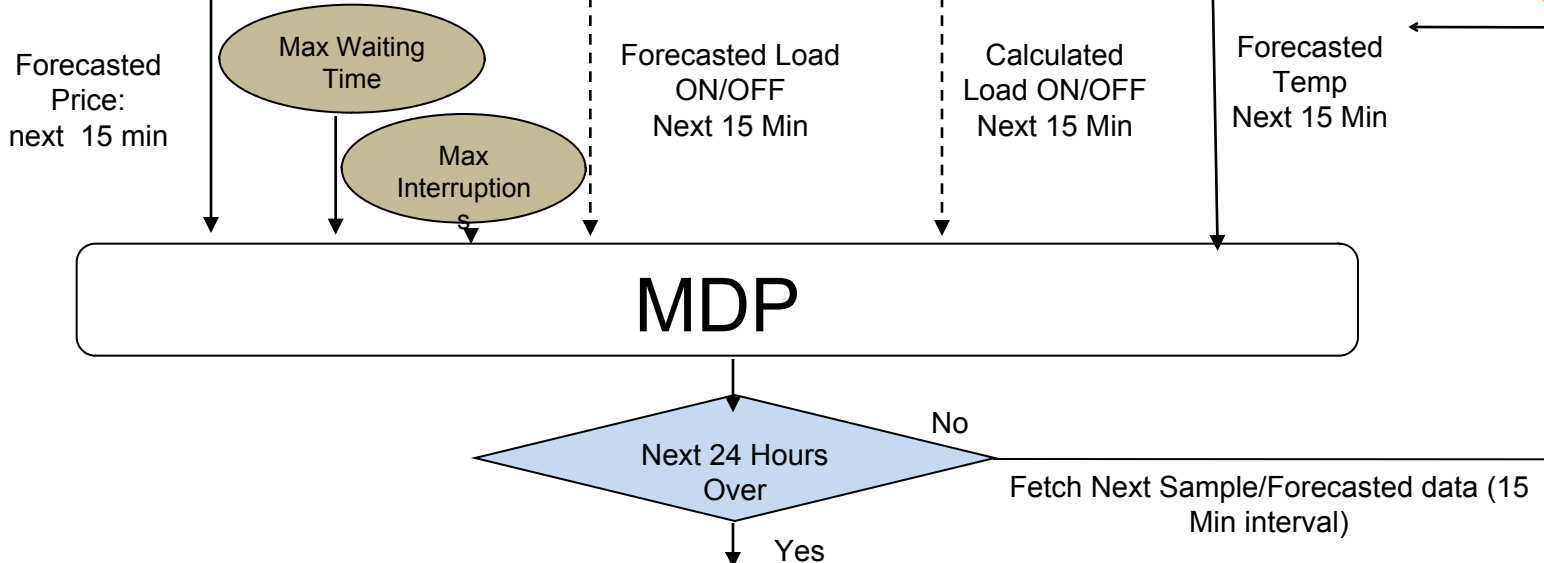


**Fig 3. HAN [3]**

Phase 1



Phase 2



Phase 3

ON/OFF schedule for Next 24 Hours : 96 Samples (1 sample = 15 Minutes Interval)



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# Prediction phase

## Price Prediction



Predictor models
Neural Network
Linear regression
Non-Linear regression
ANFIS
ARIMA

Independent variables
Minutes Of Day
Previous week Same Time Price
Average Previous Week Same Day Price
Temperature, Relative humidity, Dew point, Wind speed

## Load prediction



Predictor models
Neural Network
Linear regression
Non-Linear regression
ANFIS
ARIMA

Independent variables
Minutes Of Day
Weekend is true
Weeks Day Number
Hour Of Day
Previous week Same Time Load
Average Previous Week Same Day Load
Temperature, Relative humidity, Dew point, Wind speed

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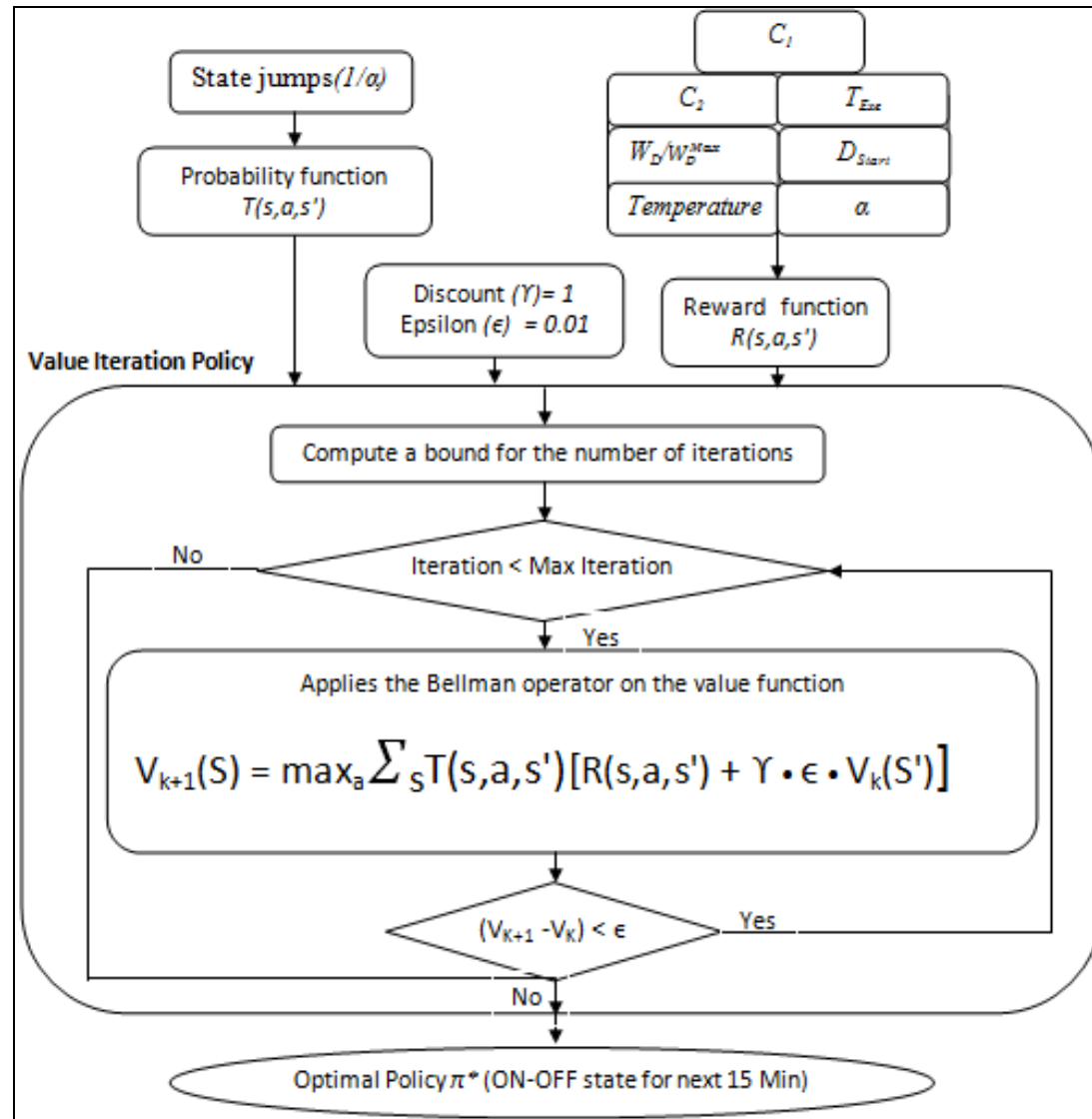
# Markov Decision Process(MDP)

Forecasted LOAD and PRICE is applied as input to MDP (Formulated as MDP problem). MDP outputs/determines, ON/OFF state of the device for next 15 Minutes.

MDP runs for every 15 Minutes.MDP determines ON/OFF state(of next 15 Minutes) based on 6 parameters and additional Temperature(If Temp Dependent Device).

- Price for next 1 hour ( $C_1$ )
- Electricity price at a specific instant of time  $t$  ( $C_2$ )
- Total device execution time left ( $T_{Exe}$ )
- Present waited time ( $W_D / W_{DMax}$ )
- Alpha: state jumps ( $\alpha$ )
- Checks, if device needs to be turned ON that day ( $D_{Start}$ )

# Key Plots : Optimization / Phase 2 implementation





# MDP : Formation of Transition Probability

The transition probability is a 5 x 5 x 2 matrix, i.e. 5 states [S1, S2, S3, S4, S5] and 2 actions [ON, OFF].

$$C_t^{total\_day} = RTP * Load = \zeta_t * \omega_{Load}$$



$$Step_{size} = Max ( C_t^{total\_day} ) / 5$$



$$T(s,a,s') = \frac{\text{Number of transisions from state } S \text{ to } S'}{\text{Total number of transistions from the state } S}$$

	State 1	State 2	State 3	State 4	State 5
State 2					
State 3					
State 4					
State 5					

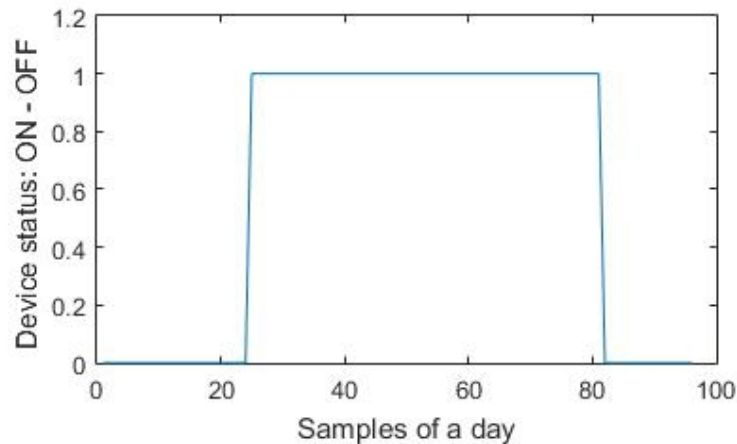
Transition probability is a 5 x 5 x 2 matrix

```
val(:, :, 2) =
    0.9737      0      0      0      0.0263
    0.2000    0.6000    0.2000      0      0
      0    0.1429    0.7143    0.1429      0
      0      0    0.1250    0.7500    0.1250
      0    0.0270      0    0.0270    0.9459
```

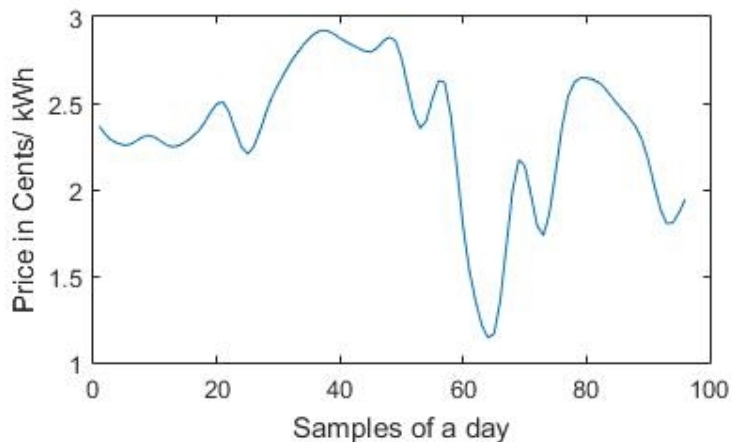
Transition probability for ON

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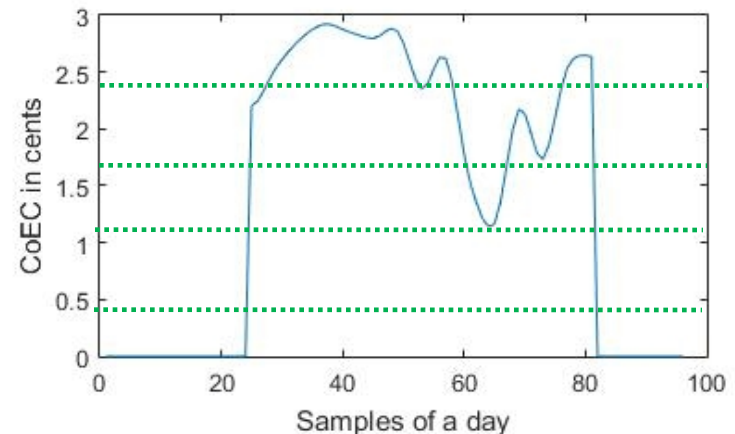
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Transition probability for ON

# MDP : Formation of Reward function

$$R = \alpha * C_1 * C_2 * T_{Exe} * \frac{W_D}{W_D^{Max}} * D_{Start} * Temperature$$

Where,

- $\alpha$  : State jump factor.
- $C_1$  : Cost for next 1 hour.
- $C_2$  : How Low is the present cost
- $T_{exe}$  : Device execution time left.
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# MDP : Formation of Reward function

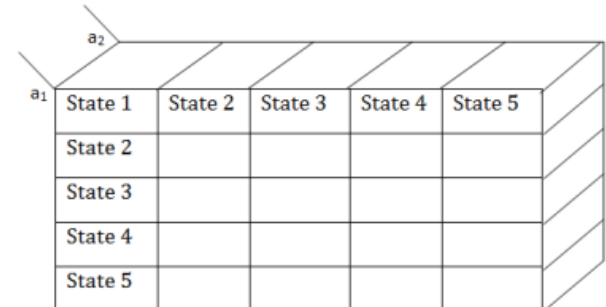
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Jump from a higher CoEC state to a lower CoEC is assigned better reward than a jump from lower to higher. Where state  $S$  is the initial state and  $S'$  is the next state. The index value ranges from 1 to 5.

$$\alpha = \frac{\text{Index of } S}{\text{Index of } S'}$$



State 1	State 2	State 3	State 4	State 5
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State 3				
State 4				
State 5				

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Temperature	: Temperature (If Temp Dependent Device).

$$H_{std(X)} = \mu + std(X)$$

$$C_1 = \sum_4 \{ True( [\omega_{Price}^{t=0}, \omega_{Price}^{t+15}, \omega_{Price}^{t+30}, \omega_{Price}^{t+45}] < H_{std(X)} ) \}$$

Where,

$\mu$ : Mean of the Forecasted price data: set of 96 samples, each sample at 15 min interval.

$std(X)$  : Standard Deviation of the Forecasted price data: set of 96 samples, each sample at 15 min interval.

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- $Temperature$  : Temperature (If Temp Dependent Device).

$$C_2 = \frac{\omega_{Price}^t - P_{Min}}{P_{Max} - P_{Min}}$$

Where,

- $\omega_{Price}^t$  : Electricity price at the current sampling time.
- $\underline{P_{Min}}$  : Minimum electricity price of the day:  $\text{Min}\{\text{set of prices:96samples}\} = \min\{\omega_{Price}\}$
- $\underline{P_{Max}}$  : Maximum electricity price of the day:  $\text{Max}\{\text{set of prices:96 samples}\} = \max\{\omega_{Price}\}$

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$T_{exe}$	: <b>Device execution time left.</b>
$W_D/W_{DMax}$	: Present waited time.
$D_{start}$	: Checks, if device needs to be turned ON that day.
Temperature	: Temperature (If Temp Dependent Device).

This reward component assigns lower reward during the devices initial execution time, thereby less curtailment on its operation. On the other hand, this reward component forces the device to remain turned ON, when the device approaches its required execution time, thereby allowing the device to execute till the completion of specific task



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A reward component for waiting time of the device. The reward increases as the device's present waiting time approaches the device's maximum waiting time

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Temperature	: Temperature (If Temp Dependent Device).

This reward component scales the reward function with '1' if at all the device is required to be scheduled/turned ON that particular day or else scales with '0'. As a consequence the scenario in which the devices being turned OFF at weekends are covered.

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- $D_{start}$  : Checks, if device needs to be turned ON that day.
- $Temperature$  : Temperature (If Temp Dependent Device).

$$Temperature = \frac{\omega_{Temperature}^t - Temperature_{Min}}{Temperature_{Max} - Temperature_{Min}}$$

Where,

$\omega_{Temperature}^t$  : Temperature at the current sampling time.

$Temperature_{Min}$  : Minimum of entire day's temperature

$Min\{set\ of\ temperature: 96samples\} = \min\{\omega_{Temperature}\}$

$Temperature_{Max}$  : Maximum of entire day's temperature

$Max\{set\ of\ temperature: 96samples\} = \max\{\omega_{Temperature}\}$

Required Load scheduling is achieved. A simulator is designed for ease of use and assessment.



SMART LOAD  
SCHEDULER

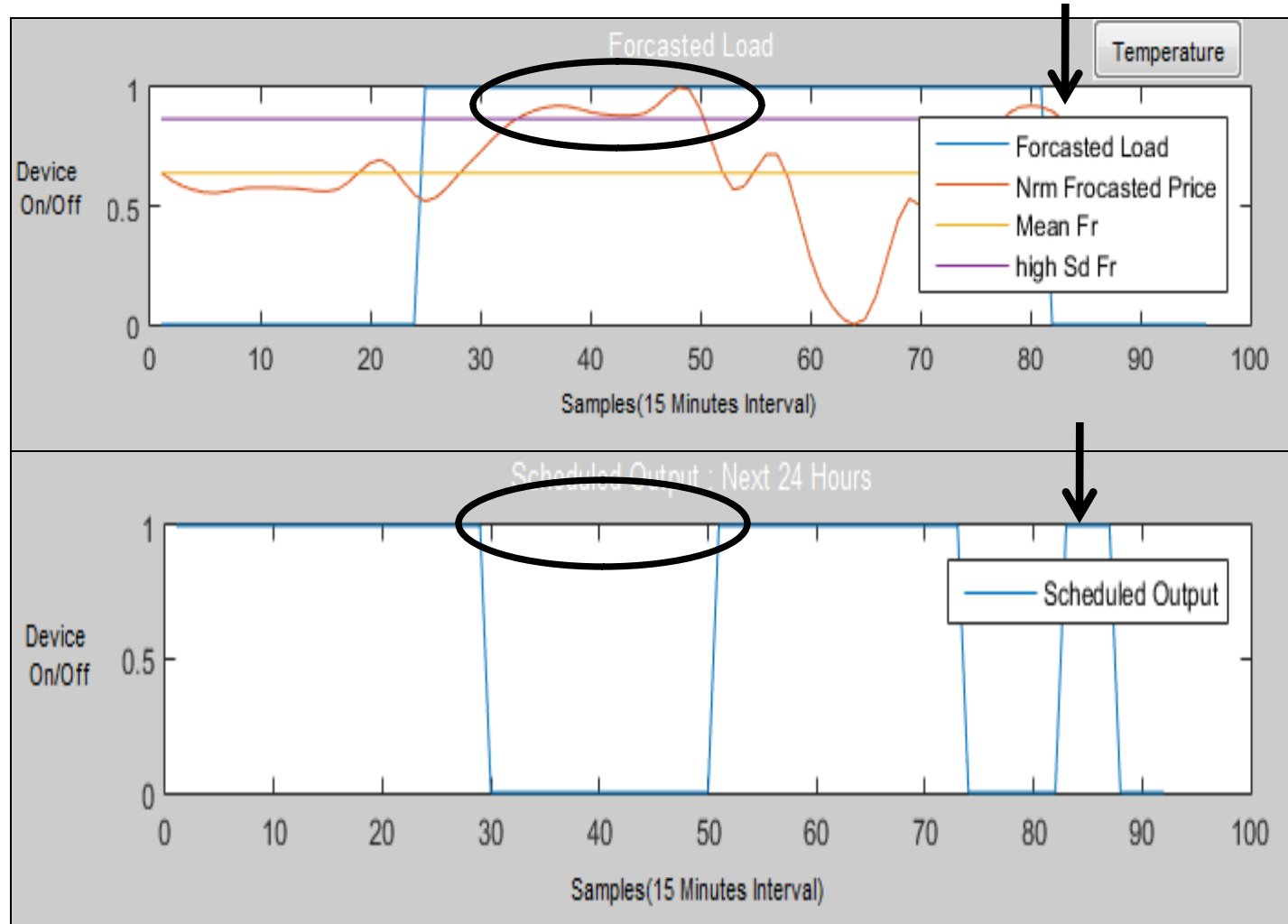


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# Functionality : Water Pump

Water Pump: Forecast Date(April 29<sup>th</sup> of 2015)

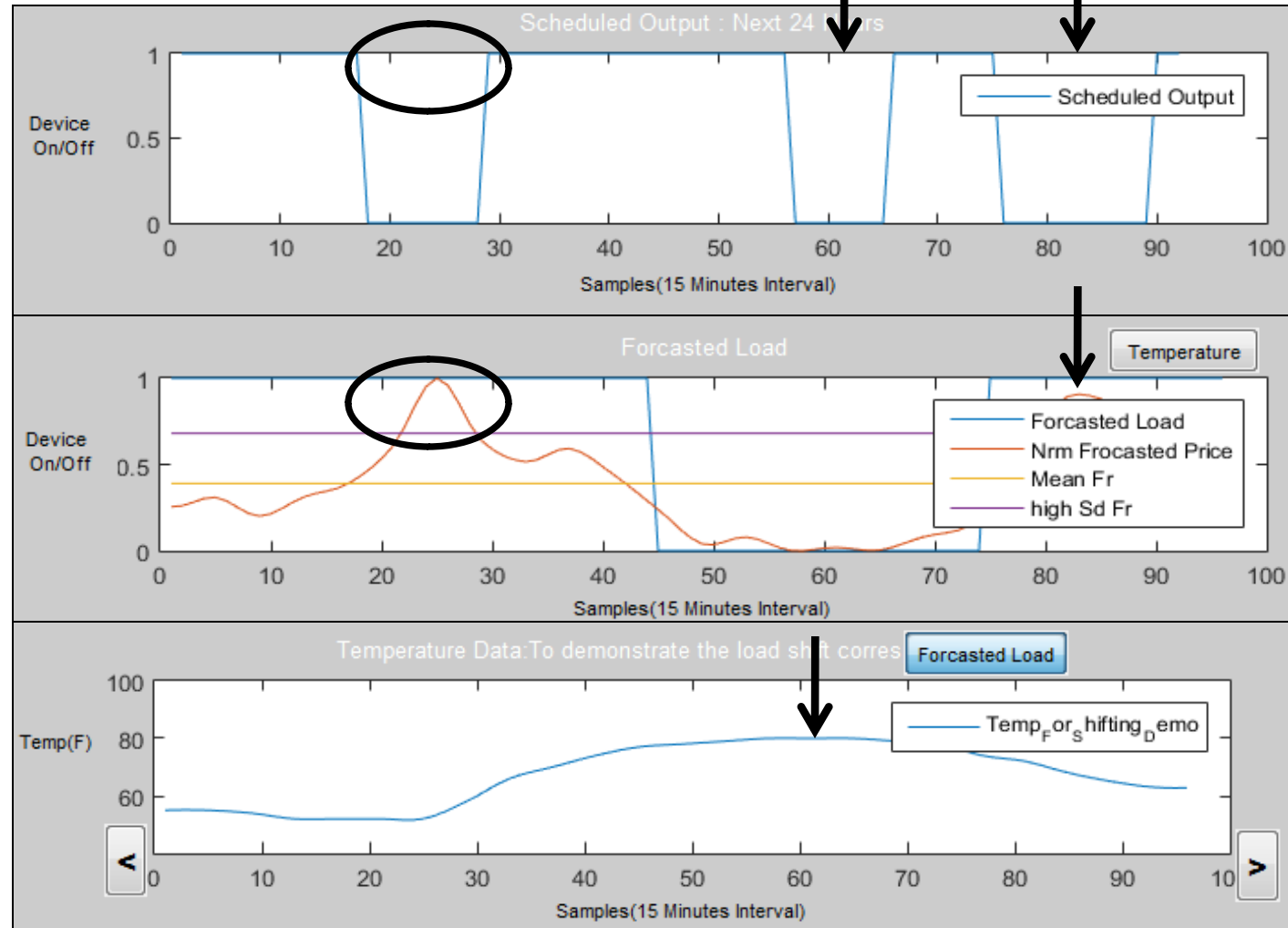
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- 4) Alpha: state jumps
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# Functionality : Heater

Heater : Forecast Date(April 29<sup>th</sup> of 2015)

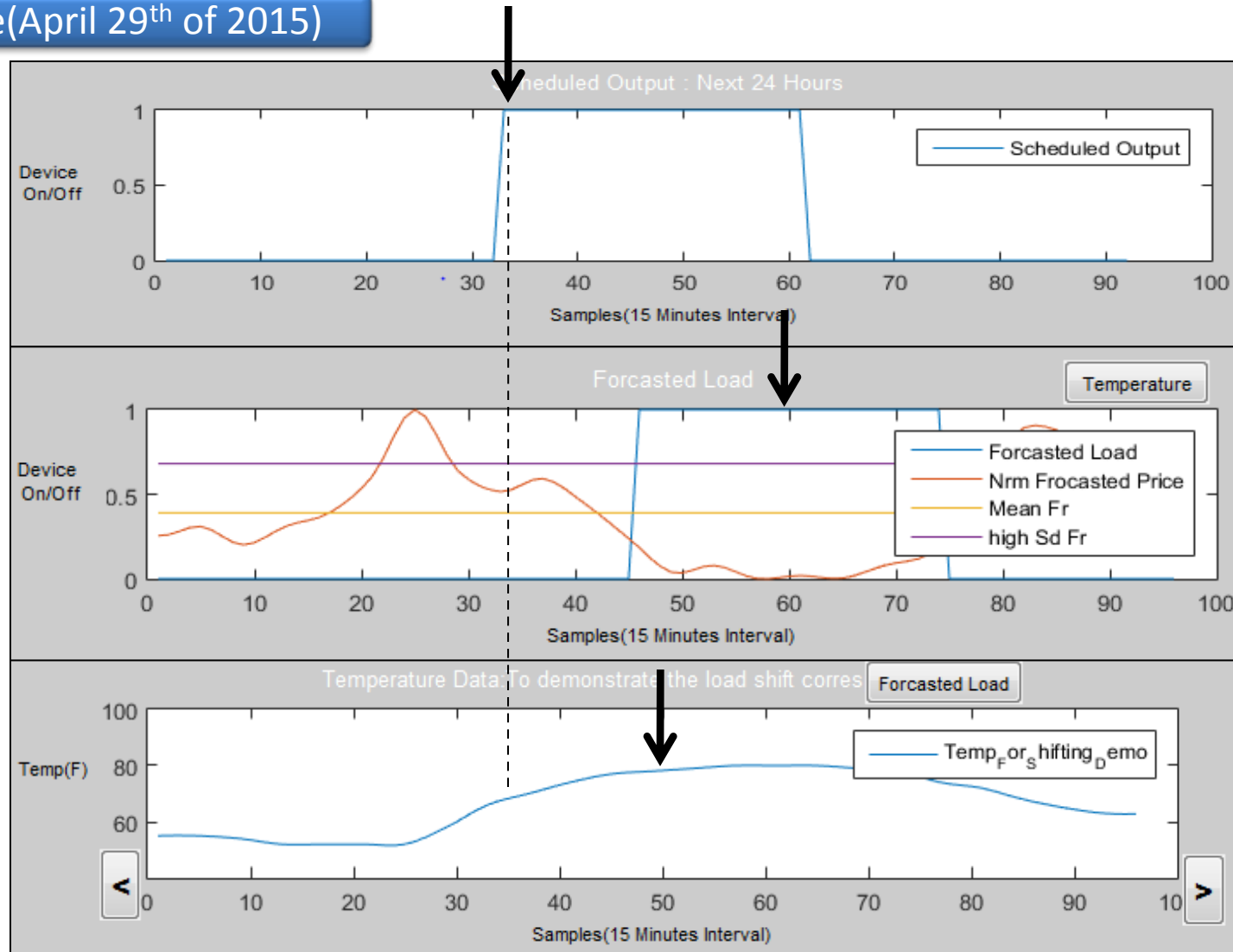
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# Functionality : Cooler

Cooler: Forecast Date(April 29<sup>th</sup> of 2015)

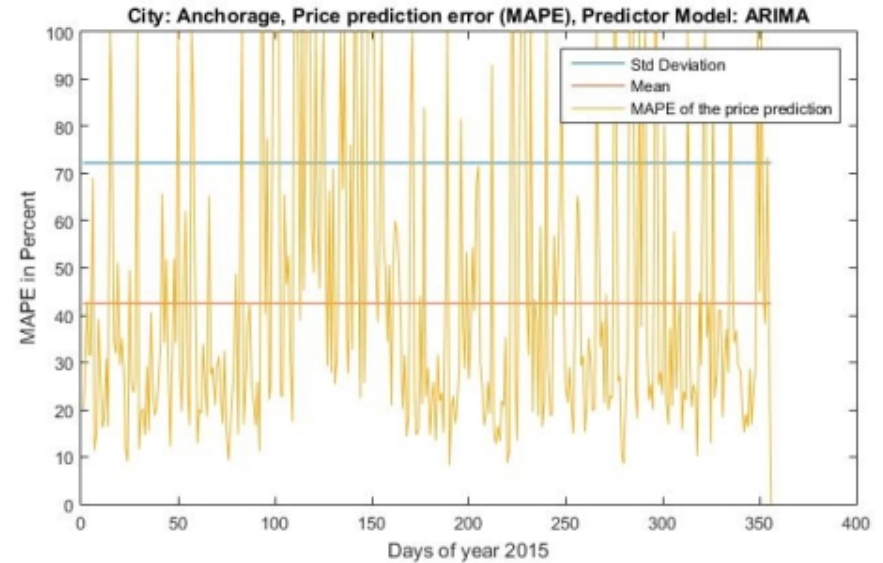
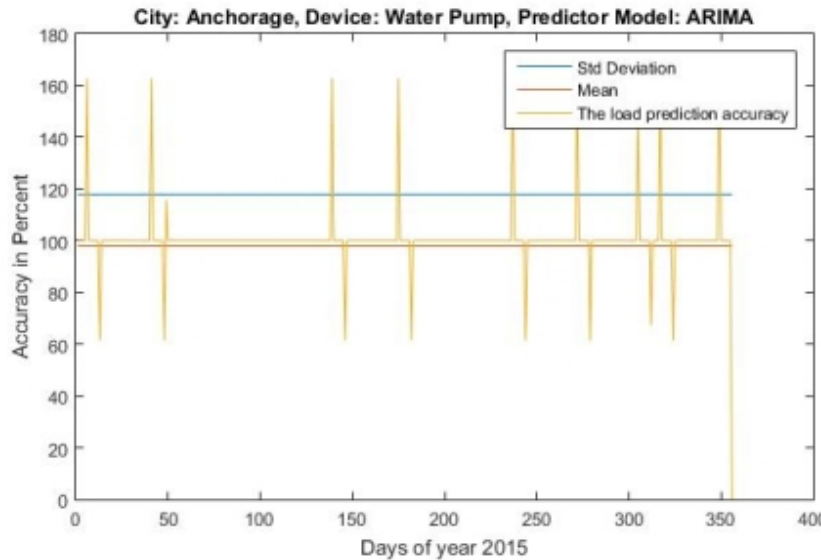
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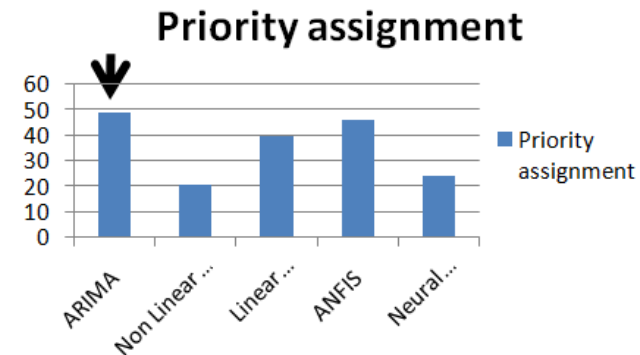
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# Performance Evaluation : Prediction



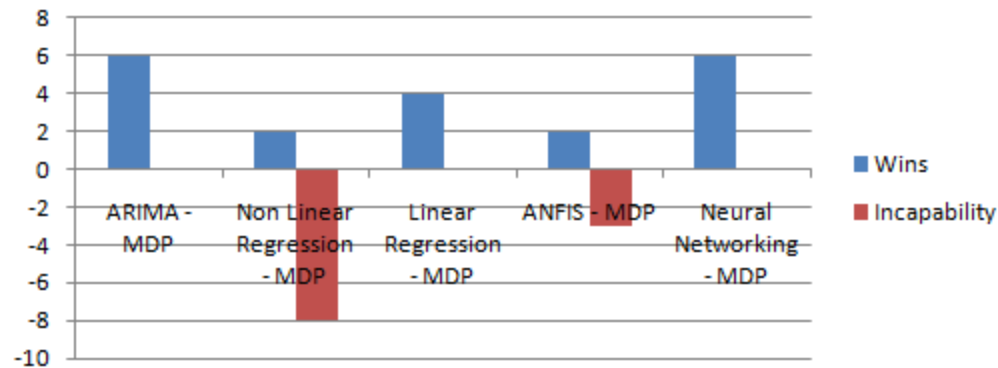
Water Pump	ANKORAGE		LITTLE_ROCK		PALMADEL	
	PRICE	LOAD	PRICE	LOAD	PRICE	LOAD
ARIMA	Mean:42.48 SD :72.72	Mean:97.94 SD :115.76	Mean:42.84 SD :72.90	Mean:97.94 SD :115.76	Mean:42.73 SD :72.13	Mean:97.94 SD :115.76
Non Linear Regression	Mean:78.91 SD :109.79	Mean:97.92 SD :115.83	Mean:78.91 SD :109.79	Mean:97.92 SD :115.83	Mean:78.91 SD :109.79	Mean:97.94 SD :115.86
Linear Regression	Mean:45.05 SD :75.07	Mean:97.80 SD :115.90	Mean:44.81 SD :74.85	Mean:97.82 SD :115.92	Mean:45.27 SD :75.27	Mean:97.80 SD :115.90
ANFIS	Mean:42.41 SD :70.51	Mean:106.70 SD :143.63	Mean:42.41 SD :70.51	Mean:106.70 SD :143.62	Mean:42.41 SD :70.51	Mean:106.40 SD :131.70
Neural Networking	Mean:54.30 SD :84.95	Mean:97.36 SD :116.31	Mean:52.61 SD :83.39	Mean:97.28 SD :115.63	Mean:52.36 SD :82.86	Mean:98.51 SD :116.65

Prediction Accuracy Evaluation winner



## MDP Evaluation

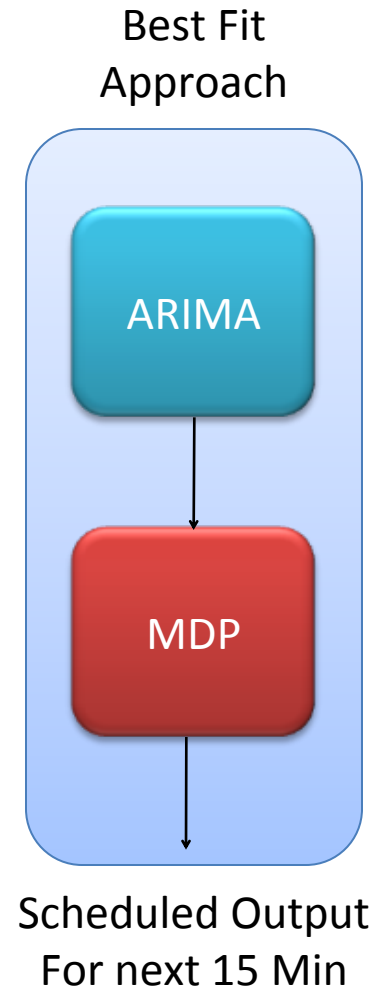
ANKORAGE						
Water pump						
29-4-15	Max Waiting Time (Samples 15 Min Interval)	Max Interruptions	MDP Scheduled ON Time (Samples 15 Min Interval)	Occurred ON Time (Without MDP) (Samples 15 Min Interval)	CoEC from MDP scheduled switching in cents	Occurred CoEC in cents
ARIMA	20	2	57	57	1.2768	1.7046
Non Linear Regression	<i>Inf</i>	<i>Inf</i>	<i>Inf</i>	<i>Inf</i>	<i>Inf</i>	
Linear Regression	20	2	57	57	1.2979	
ANFIS	<i>Inf</i>	<i>Inf</i>	<i>Inf</i>	<i>Inf</i>	<i>Inf</i>	
Neural Networking	10	2	57	57	1.2934	



**Table 1.** Majority winner by providing best price for different scenarios

Winners	USA_AK_ANKORAGE	USA_AK_LITTLE_ROCK	USA_AK_PALMADEL
Water Pump	ARIMA	ARIMA	ARIMA
Heater	ARIMA	ARIMA	ARIMA
Cooler	ARIMA	ARIMA	ARIMA

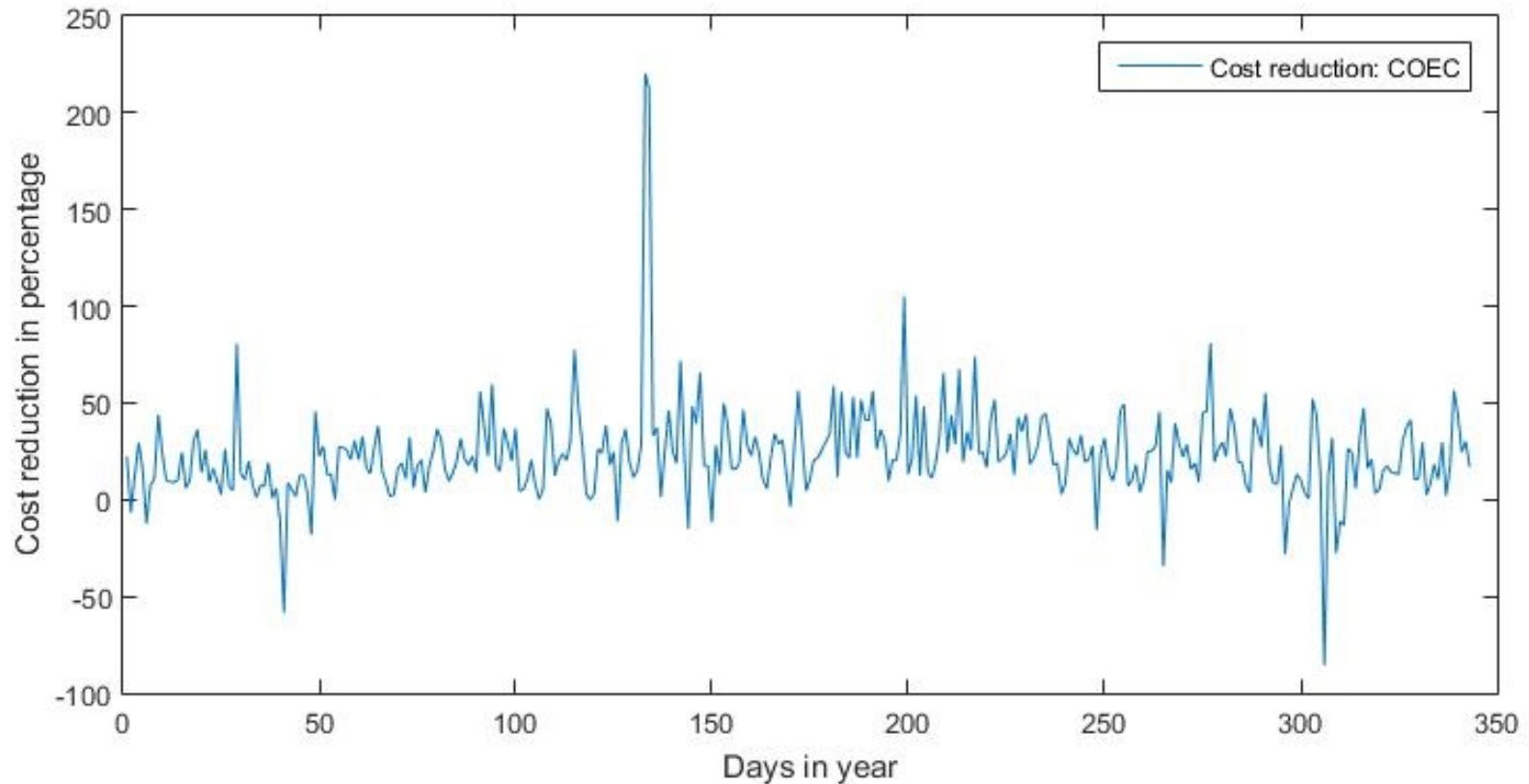
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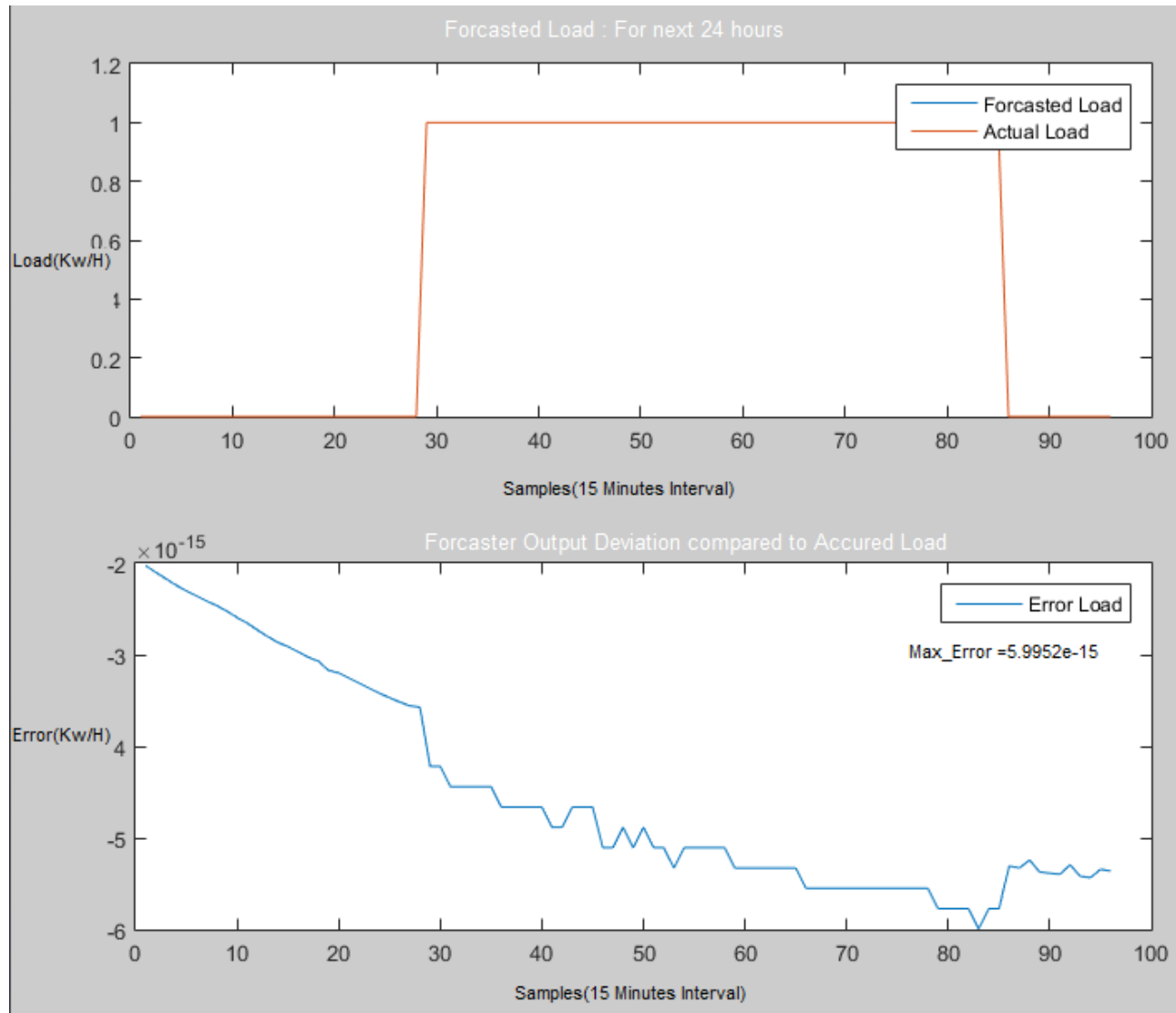


THANK  
**YOU**

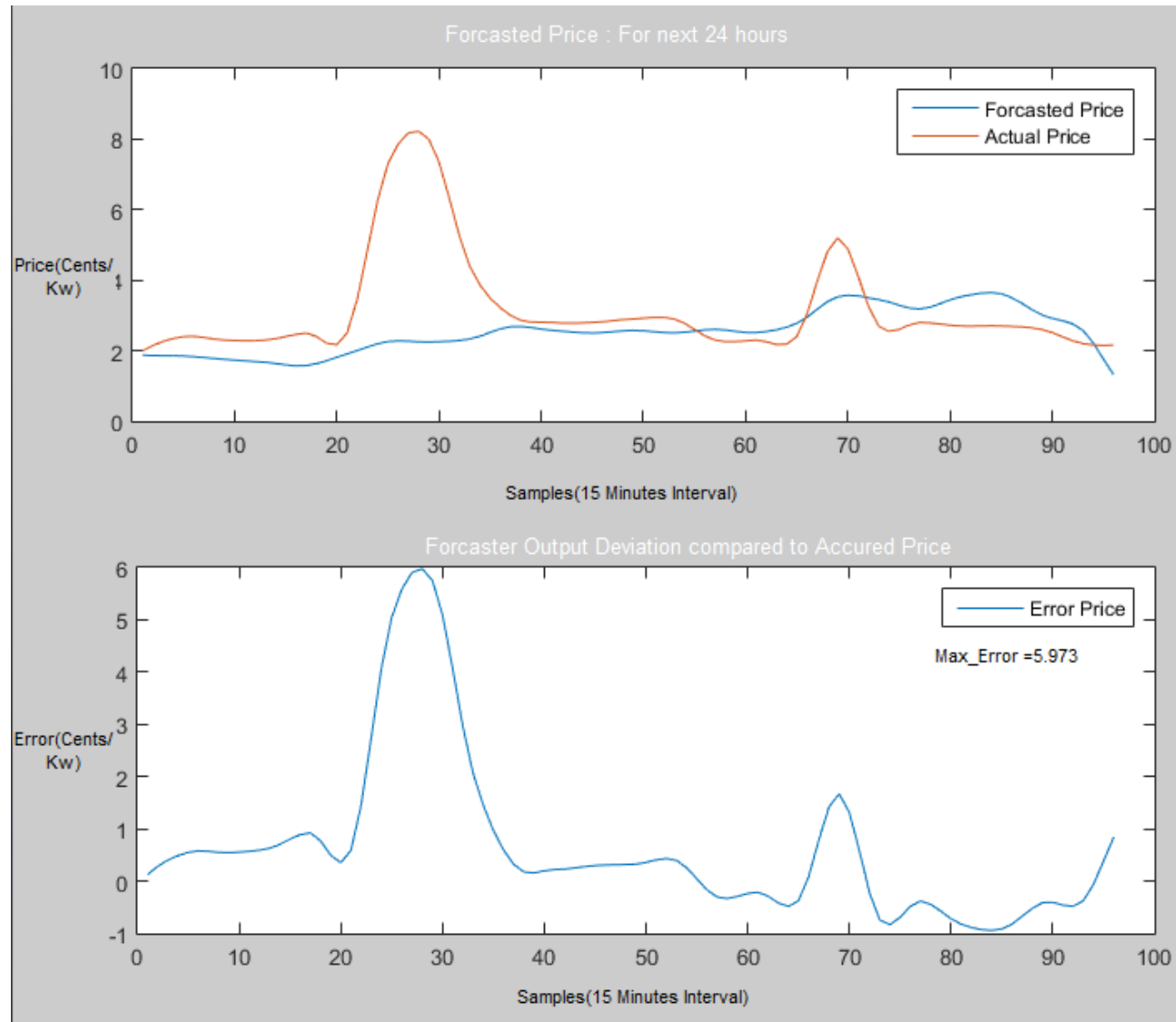
# Key Plots : COEC or Cost reduction



# Key Plots : Load prediction



# Key Plots : Price prediction





- [1] *Smart grid* , Accessed on: 4-4-2017,under the address: <https://www.edsoforsmartgrids.eu/home/why-smart-grids/>
- [2] *Smart grid* , Accessed on: 4-4-2017,under the address: [http://www.naonworks.com/old/inc\\_html/sub2\\_3.html](http://www.naonworks.com/old/inc_html/sub2_3.html)
- [3] *Smart meters* , Accessed on: 4-4-2017,under the address: <https://www.sdge.com/residential/about-smart-meters/home-and-business-area-network>
- [4] *Geir Warland, Birger Mo : "Stochastic optimization model for detailed long-term hydro thermal scheduling using scenario-tree simulation". SINTEF Energy Research, Sem Sælands vei 11, Trondheim 7034, Norway.*
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